

Proof Theory and Logic in Law

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Mathematical Logic: Proof Theory, Constructive Mathematics
Oberwolfach

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Proof assistants and type theory

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- Provide reasoning using lambda terms using some 'combinatorial logic' where combinators correspond to linguistic elements ?

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Article 4 (i): 'a week' means the period of time between 00.00 on Monday and 24.00 on Sunday.

Article 4 (k): 'daily driving time' means the total accumulated driving time between the end of one daily rest period and the beginning of the following daily rest period or between a daily rest period and a weekly rest period;